

IV Semester B.C.A. Examination, September/October 2022 (CBCS) (F+R) (2015 – 16 and Onwards) COMPUTER SCIENCE

BCA 405: Operations Research

Time: 3 Hours

Max. Marks: 100

Instruction: Answer all the Sections.

SECTION - A

I. Answer any ten of the following:

 $(10 \times 2 = 20)$

- 1) What is Operations Research?
- 2) Write the standard form of linear programming problem.
- 3) Define slack and surplus variable.
- 4) What are transportation problems?
- 5) Define basic feasible solution and optimum solution in transportation problems.
- 6) What are the different methods of solving assignment problems?
- 7) How do you convert maximization problem to minimization for solving assignment problems?
- 8) Explain Fulkerson's rules.
- 9) Define optimistic time and pessimistic time.
- 10) What are the applications of PERT/CPM?
- 11) Define saddle point and value of the game.
- 12) What are the different methods available to solve games with mixed strategies?

SECTION - B

II. Answer any four of the following :

 $(4 \times 10 = 40)$

13) a) Explain phases of operations research.

b) A company produces two types of leather belts, type-A and type-B. Profits on two types of belts are Rs. 40 and Rs. 30 respectively per belt. Each belt of type-A requires twice as much time required for a belt of type-B and the company could produce 1000 belts per day. But the supply of leather is sufficient only for 800 belts per day. Belt of type-'A' requires a fancy buckle and only 400 fancy buckles are available for this, per day. For belt of type-B, only 700 buckles are available per day. Formulate the problem as LPP.

P.T.O.



- 14) a) Explain the steps involved in graphical solution to LPP.
- 5

b) Solve the following LPP by graphical method:

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Maximize,
$$z = 2x_1 + 3x_2$$

Subject to $2x_1 + x_2 \le 12$
 $x_1 + 3x_2 \le 15$

- $x_1, x_2 \ge 0.$
- 15) Determine the initial basic feasible solution to the following transportation problem using
 - a) North-West Corner Method

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b) Vogel's Approximation Method.

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| | | | Destii | nation | 3000 | Supp |
|--------|------|----|--------|--------|------|------|
| | | 1 | 2 | 3 | 4 | |
| | 1 | 21 | 16 | 15 | 3 | 11 |
| Source | 2 | 17 | 18 | 14 | 23 | 13 |
| | 3 | 32 | 27 | 18 | 41 | 19 |
| Demand | 74.0 | 6 | 10 | 12 | 15 | |

16) a) Explain Hungarian method for solving assignment problem.

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 Find the optimal assignment schedule for given table with cost of each job on each machine.

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Machine

| | | W | X | Υ | Z |
|-----|---|----|----|----|----|
| | A | 18 | 24 | 28 | 32 |
| Job | B | 8 | 13 | 17 | 18 |
| | Č | 10 | 15 | 19 | 22 |
| | | | | | |

17) The following table gives the list of activities and duration in hours:

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| Job | 1 – 2 | 1 – 3 | 1 – 4 | 2 – 5 | 3 – 4 | 3 – 7 | 4 – 5 | 4 – 6 | 5 – 6 | 4 – 7 | 6 – 7 |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Duration | 20 | 24 | 8 | 20 | 16 | 24 | 0 | 18 | 0 | 4 | 12 |

- 1) Draw the arrow diagram.
- For each activity calculate early start and early finish time. Latest start and latest finish time.
- 3) Calculate Total Float (TF) and Free Float (FF).

18) a) Explain pay off matrix and strategy.

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b) Solve the following game. Find the optimal strategy of Player A and Player B.

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| | | Player B | | | |
|----------|-----|----------|----|-----|--|
| | | 1 | 11 | 111 | |
| | 1 | -3 | -2 | 6 | |
| Player A | 11 | 2 | 0 | 2 | |
| | 111 | 5 | -2 | -4 | |

SECTION - C

III. Answer any four of the following:

 $(4 \times 10 = 40)$

19) Solve the following LPP by simplex method:

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Maximize,
$$z = 3x_1 + 2x_2 + 5x_3$$

Subject to $x_1 + 4x_2 \le 420$
 $3x_1 + 2x_3 \le 460$
 $x_1 + 2x_2 + x_3 \le 430$.

20) a) Explain the steps involved in matrix-minima method.

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b) Solve the following transportation problem by Least Cost Method.

| 1 | | T | o | | Supply |
|--------|----|----|----|----|--------|
| | 10 | 20 | 5 | 7 | 10 |
| | 13 | 9 | 12 | 8 | 20 |
| Erom | 4 | 5 | 7 | 9 | 30 |
| From | 14 | 7 | 1 | 0 | 40 |
| 41 | 3 | 12 | 5 | 19 | 50 |
| Demand | 60 | 60 | 20 | 10 | - |

b) Solve the transportation problem using MODI method.

- 21) a) Write the difference between transportation problem and assignment problem.



22) a) Find the optimal assignment for the following problem:

| | Α | В | C | D |
|---|----|----|----|----|
| W | 41 | 72 | 39 | 52 |
| X | 22 | 29 | 49 | 65 |
| Υ | 27 | 39 | 60 | 51 |
| Z | 45 | 50 | 48 | 52 |

b) Write the difference between PERT and CPM.

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23) a) Explain the different phases of project-scheduling by PERT/CPM.

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b) Draw the network diagram for the following data:

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| Job | Predecessor | | | |
|-----|------------------|--|--|--|
| Α | _ | | | |
| В | 1 - 2 | | | |
| С | Α | | | |
| D | Α | | | |
| Е | B, C | | | |
| F | Α | | | |
| G | F | | | |
| Н | D, E | | | |
| 1 | G, H | | | |
| J | G, H | | | |
| K | G, H | | | |
| L | J, K, L | | | |
| М | J, K, L | | | |
| N | K, J | | | |

24) Use the dominance principle to solve the following game.

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Player B